

UNIVERSITY OF THE WEST INDIES  
CAVE HILL CAMPUS

*Department of Computer Science, Mathematics & Physics*

**ELET2230 - Digital Communications 1**

**Assignment 2**

**Due: December 5, 2020**

1. If a transmitted BPSK signal  $s_1(t) = \cos(20\pi t)$  is of duration 0.5 seconds determine:
  - (a) The amplitude of the signal and its carrier frequency. [3]
  - (b) Energy per binary digit  $E_b$  [2]
  - (c) Coordinates of the signal points at the receiver under a noiseless channel [2]

2. Given that BPSK signals are  $s_1(t) = \sqrt{E_b} \cdot \phi_1(t)$  and  $s_2(t) = -\sqrt{E_b} \cdot \phi_1(t)$ , where  $\phi_1 = \sqrt{\frac{2}{T_b}} \cos(2\pi f_c t)$ , Derive the following expression for the probability of an error in a binary digit  $P_b = Q\left(\sqrt{\frac{2E_b}{N_o}}\right)$ , where  $E_b$  is the energy per binary digit,  $N_o$  is the single sided noise spectral power density,  $T_b$  is the symbol duration and  $f_c$  is the carrier frequency. [8]

Hence show that if the BPSK modulator is replaced by a QPSK modulator, then  $P_b$  for QPSK is given by  $\left(\alpha - \frac{\alpha^2}{2}\right)$  [5]

3. Consider a BPSK demodulator that utilizes an 8-level soft-decision output. Derive an expression for the forward transition probability  $P(4|0)$  [8]

Explain how one could determine this forward transition probability  $P(4|0)$  by simulation [2]